

# Additional Mathematics Notes

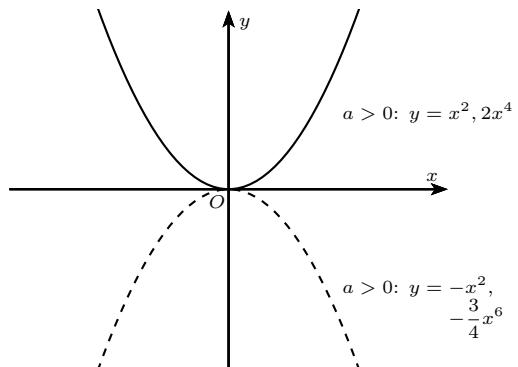
## (Graphs)

Reproduced from <http://teach.sg>

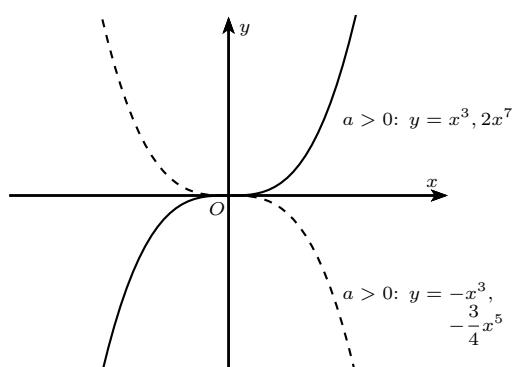
### 1 Power Functions

Graphs of power functions ( $y = ax^n$ )

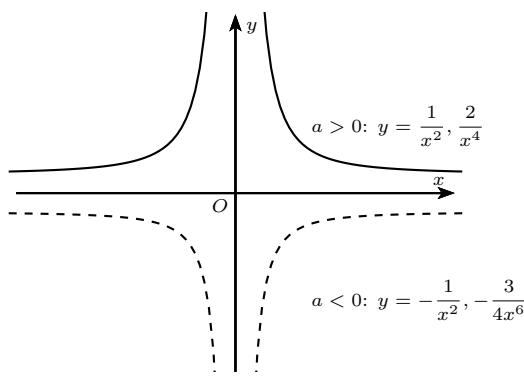
$$n = 2, 4, 6, 8, \dots$$



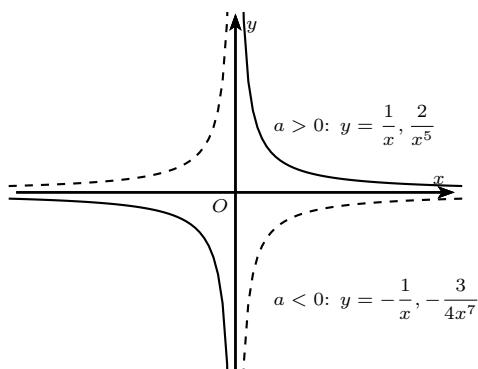
$$n = 3, 5, 7, 9, \dots$$



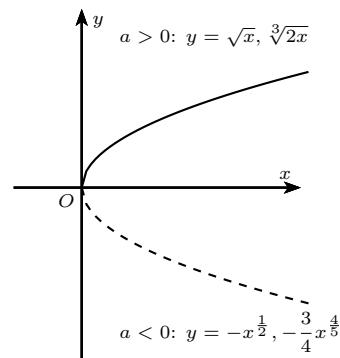
$$n = -2, -4, -6, -8, \dots$$



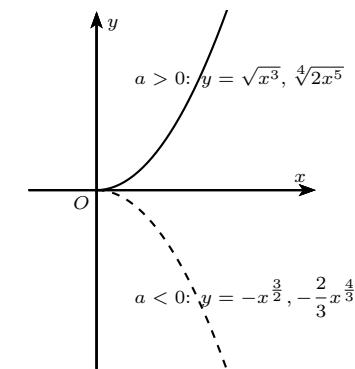
$$n = -1, -3, -5, -7, \dots$$



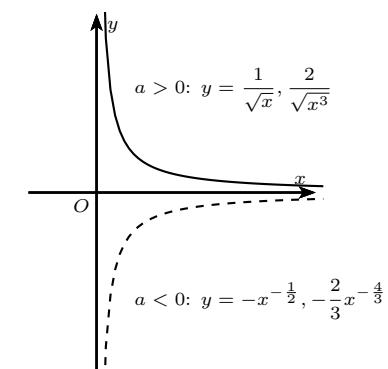
$$x > 0, 0 < n < 1$$



$$x > 0, n > 1$$



$$x > 0, n < 0$$

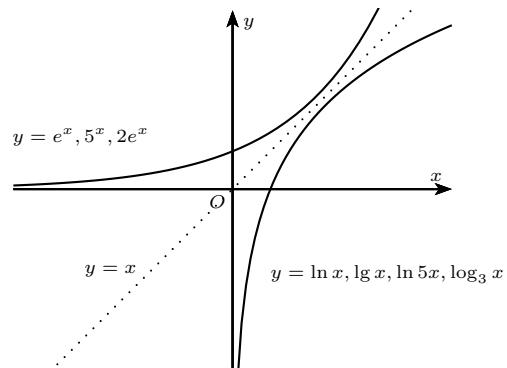


## 2 Exponential & Logarithmic Function (Graphs)

Graphs of exponential & logarithmic function

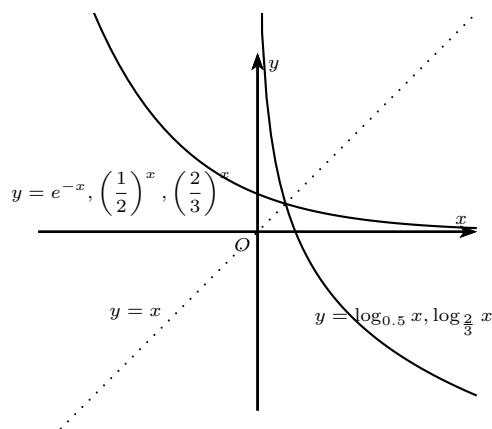
$$y = e^x, a^x, a > 1$$

$$y = \ln x, \log_a x, a > 1$$

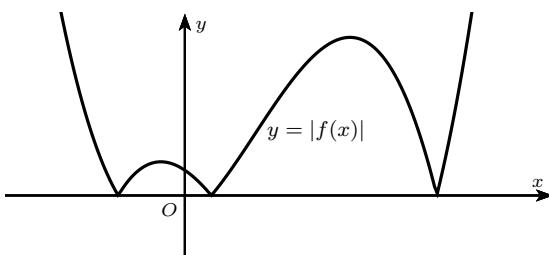
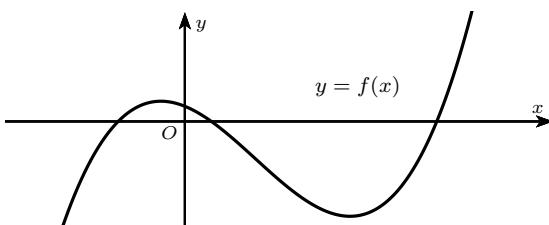


$$y = e^{-x}, a^x, 0 < a < 1$$

$$y = \log_a x, 0 < a < 1$$



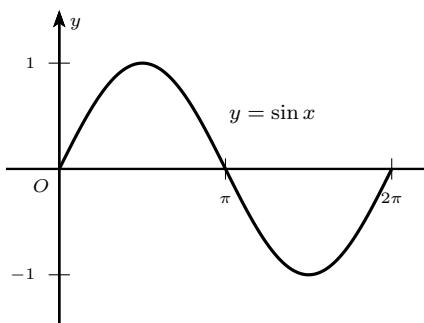
## 3 Modulus Functions Graphs



As can be seen, all the negative portions below the  $x$ -axis is reflected in the  $x$ -axis when the modulus function is applied.

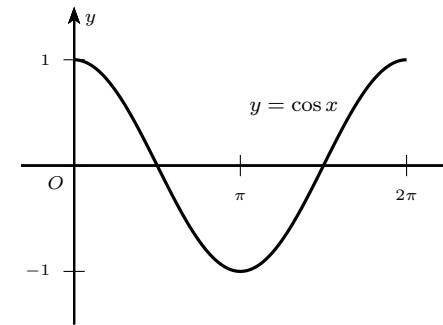
## 4 Trigonometric Graphs

Sine graph



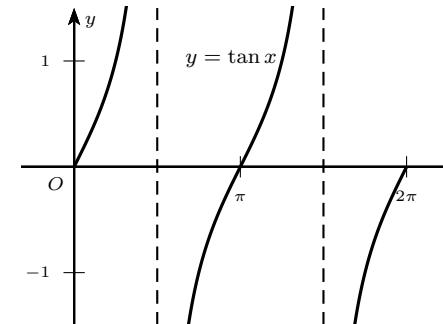
1. amplitude = 1
2. period =  $2\pi$

Cosine graph



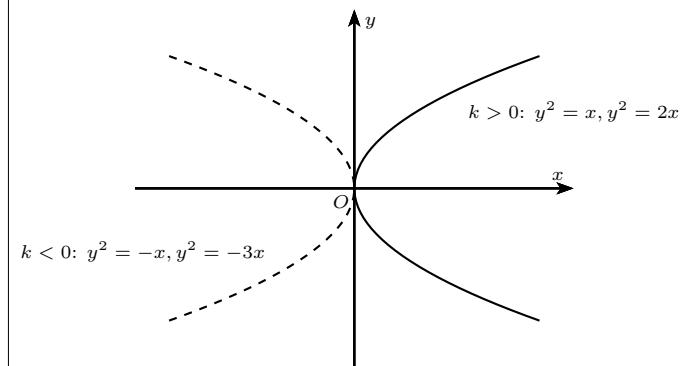
1. amplitude = 1
2. period =  $2\pi$

Tangent graph



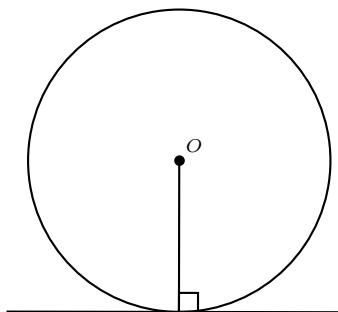
period =  $\pi$

## 5 Graphs Of Parabolas ( $y^2 = kx$ )

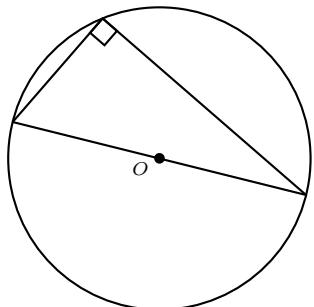


## 6 Proofs In Plane Geometry

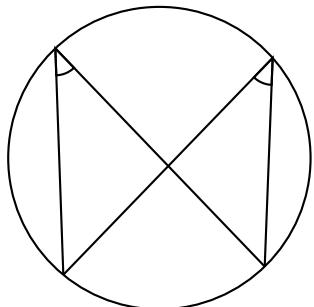
### Properties Of Circles



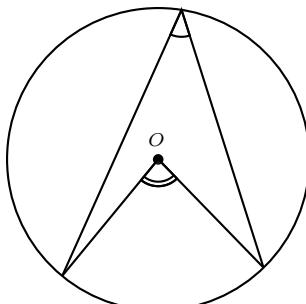
tan.  $\perp$  rad.



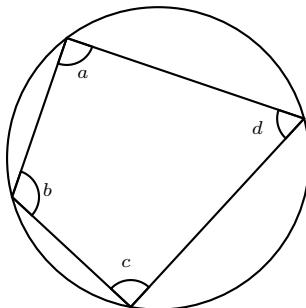
rt.  $\angle$  in semicircle



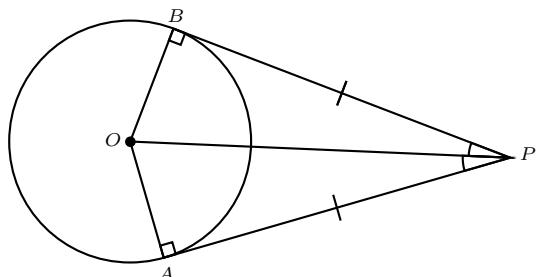
$\angle$ s in same seg.



$\angle$  at centre = 2  $\angle$  at circ.



$\angle$ s in opp. seg. ( $a + c = b + d = 180^\circ$ )

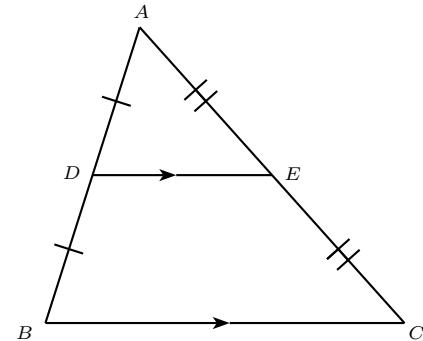


tan. from ext. pt.

### Congruent & Similar Triangles

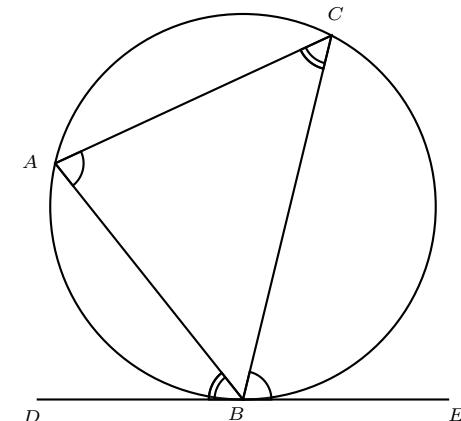
Congruent triangles	Similar triangles
SSS, SAS, AAS, RHS	SSS, SAS, AAA

### Midpoint Theorem



If  $D$  and  $E$  are the midpoints of  $AB$  and  $AC$  respectively, then  $DE \parallel BC$  and  $DE = \frac{1}{2}BC$ .

### Tangent-Chord Theorem (Alternate Segment Theorem)



If  $DE$  is a tangent to the circle at  $B$ , then  $\angle CAB = \angle CBE$  and  $\angle ACB = \angle ABD$ .